

The Diederich-Fornæss index and its applications

Siqi Fu

Rutgers University-Camden
E-mail: sfu@rutgers.edu

Abstract

Diederich and Fornæss showed in 1977 that for any bounded pseudoconvex domain Ω with C^2 -boundary in a Stein manifold, there exist a positive constant η and a defining function r such that $-(-r)^\eta$ is strongly plurisubharmonic on Ω . The Diederich-Fornæss exponent η has found many applications in several complex variables, including the mapping problem and L^2 -estimate of the $\bar{\partial}$ -operator. In this talk, we will discuss these applications and especially its connection with non-existence of Stein domains with Levi-flat boundaries in complex manifolds. This talk is based in part on joint work with Mei-Chi Shaw.